Concrete plays a vital role in the design and construction of the infrastructure. To meet the global demand of concrete in future, it is becoming a challenging task to find suitable alternatives to natural aggregates. Steel slag is a by-product of steel making process. The steel slag aggregates are characterized by studying particle size and shape, physical and chemical properties, and mechanical properties as per IS: 2386-1963. The characterization study reveals the better performance of steel slag aggregate over natural coarse aggregate. M30 grade of concrete is designed and natural coarse aggregate is completely replaced by steel slag aggregate. Packing density of aggregates affects the characteristics of concrete. The present paper proposes a fuzzy system for concrete mix proportioning which increases the packing density. The proposed fuzzy system have four sub fuzzy system to arrive compressive strength, water cement ratio, ideal grading curve and free water content for concrete mix proportioning. The results show, the concrete mix proportion of the given fuzzy model agrees with IS method. The comparison of results shows that both proposed fuzzy system and IS method, there is a remarkable increase in compressive strength and bulk density, with increment in the percentage replacement of steel slag.

**Keywords:** Steel slag, characterisation, packing density, fuzzy system, compressive strength, bulk density

### 1. Introduction

Concrete mix design is a procedure to arrive the proportions of the ingredients like, cement, water, coarse aggregate, fine aggregate. To achieve economy in construction, industrial by products are supplemented for the ingredients of concrete. Steel slag is a byproduct of steel making process. Steel slag can be replaced as fine aggregate and coarse aggregate.

Increased percentage of aggregates in concrete inhibits maximum volume and also the higher strength (Neville, 1983). An aggregate with wide range of particles increases the packing density. Therefore, it is beneficial to intensify the particle packing in concrete mix design, which aims to achieve densest mix, minimize the number of voids and increase the aggregate volume without affecting the concrete properties.

Fuzzy logic gives a regular calculus and performs numerical computation accessing linguistic labels stimulated by membership functions. Today fuzzy logic has been used to solve many civil engineering problems.

Previously there are many works are carried out to propose particle packing model for aggregate. This paper aims to access the effect of particle packing using fuzzy logic, in concrete containing steel slag aggregates as coarse aggregate.

### 2. Background

T. Sowmiya (2004) studied the optical basicity of slags and concluded the presence of high CaO in steel slag by studying the microstructural properties [1].

Y. Kirillidi (2005) suggested that due to its hydraulic properties, in the light concrete for the construction of the base of roads and to produce an anti-slippery blacktop material replacing 100% the limestone aggregates [2].

Jigar P. Patel (2006) concluded that the compressive strength, flexural strength and split tensile strength for steel slag aggregate concrete were similar to conventional concrete [3]. Mohammed Nadeem (2012), revealed improvement of compressive strength, split tensile and flexure strength over control mixes by 4 to 8%. The replacement of 100% slag aggregate (coarse) increased concrete density by about 5 to 7% compared to control mix [4].

I. Netinger (2012) concluded that at higher temperatures, steel slag exhibits mineral transformation followed by unstable volumetric expansion which reflected negatively on the residual properties of slag based concrete mixtures [5].

K.G. Hiraskar (2013) revealed that the compressive strength of Blast Furnace Slag aggregate concrete is found to be higher than that of conventional concrete at the age of 90 days. It has also reduced water absorption and porosity beyond 28 days in comparison to that of conventional concrete with stone chips used as coarse aggregate [6].
Dr. K. Chinnaraj (2013) studied that by replacing about 60 percent of steel slag aggregates for coarse aggregate and 40 percent of ecosand for fine aggregate will not have any adverse effect on the strength of the concrete [7].

Sultan A. Tarawneh (2014) by thorough investigation of the results have indicated that the amount of increase in compressive strength at age of 7 days are much more than that of age 28 days for all types of aggregate replacement. This indicates that the added slag could work as accelerator at early age while at 28 days age; the effect is reduced [8].

Khalid Raza (2014) suggested that the use of iron slag in concrete could enhance the strength in concrete [9].

Parviz Ghoddousi et al. (2015) reviewed that better packing of aggregates improves the strength, durability, elastic modulus and creep of the concrete. Accordingly, by increasing packing density and decreasing cement content, environment pollution will decrease. The proposed system utilizes four sub-fuzzy systems to quantify the target compressive strength, water-to-cement ratio, ideal grading curve and free water of the concrete [10].

Thomas H. Bleeck (2011) investigated that an effective approach was developed optimize the particle packing of aggregates and powders in the concrete mix design with the aim to increase the aggregate proportions used by minimizing the number of voids and increasing the density of the concrete [11].

3. Material properties

3.1. Cement

Ordinary Portland cement (Ultratech 43 Grade) confirming to IS: 8112-1989 was used throughout the investigation.

3.2. Sand (Fine Aggregate)

Locally available river sand passing through 4.75 mm sieve as per IS: 383-1970 provisions were used as fine aggregates. The physical property of fine aggregate is shown in Table 1.

<table>
<thead>
<tr>
<th>Description</th>
<th>Fine aggregate</th>
</tr>
</thead>
<tbody>
<tr>
<td>Specific gravity</td>
<td>2.6</td>
</tr>
<tr>
<td>Water absorption</td>
<td>1.57%</td>
</tr>
<tr>
<td>Fineness modulus</td>
<td>3.1 (zone II)</td>
</tr>
<tr>
<td>Surface moisture</td>
<td>Nil</td>
</tr>
<tr>
<td>Bulk density</td>
<td>1450 kg/m³</td>
</tr>
</tbody>
</table>

3.3. Coarse Aggregates [Natural]

Machine crushed locally available hard granite, well graded 20 mm and down sized was used for preparation of concrete.

3.4. Steel Slag

This slag is a by-product from steelmaking processes in which the components of pig iron and steel-scrap are modified in order to produce steel that is highly valued for excellent toughness and workability. For every ton of steel production, about 200 kg of slag is generated. In JSW Steel Ltd., Salem Works (JSWS), India, 12000-13000 tons of steel Slag is produced per month and 2, 00,000 m³-3, 00,000 m³ steel slag is produced annually.

4. Methods of test for coarse aggregate for concrete

The characteristics of concrete mainly depend upon the properties of materials used. Grading, mineralogical composition, shape and texture of the aggregate affects the fresh and hardened properties of concrete. Therefore, it is necessary to study the characteristics of materials used in concrete to obtain a good quality concrete. To characterize the steel slag, the following tests were conducted as per Indian Standard (IS: 2386-1963) methods and compared with the properties of natural aggregates.

i. Particle Size and Shape
   - Sieve analysis
   - Determination of flakiness index
   - Determination of elongation index
   - Determination of angularity number

ii. Determination of light weight particles

iii. Physical Properties
   - Determination of specific gravity and water absorption
   - Determination of bulk density

iv. Mechanical Properties
   - Determination of Aggregate Crushing value
   - Determination of the 10 percent Fines Value
   - Determination of Aggregate Impact Value
   - Determination of Aggregate Abrasion Value
   - Determination of Aggregate Attrition Value

v. Chemical Test

4.1. Particle size and shape

The ungraded steel slag obtained from steel industries, is graded and it conforms to IS: 383-1970.

It is seen from the TABLE 2, the flakiness index of steel slag is lower than the natural aggregates which shows that the steel slag particles are thicker than that of the natural coarse aggregate. The elongation index of steel slag is a little higher than that of natural aggregate, it implies slag particles are shorter than natural coarse aggregate.

Angularity or absence of rounding of the particles of an aggregate is a property which is of importance because it effects the ease of handling of a mixture of aggregate and binder, for example the workability of concrete, or the stability of mixtures that rely on the interlocking of the particles. It is observed that
the angularity number is same for steel slag and natural coarse aggregate from the Table 2.

<table>
<thead>
<tr>
<th>Test</th>
<th>Natural Coarse Aggregate</th>
<th>Steel Slag</th>
</tr>
</thead>
<tbody>
<tr>
<td>Flakiness index</td>
<td>22.2%</td>
<td>8%</td>
</tr>
<tr>
<td>Elongation index</td>
<td>52.5%</td>
<td>41%</td>
</tr>
<tr>
<td>Angularity number</td>
<td>20.83</td>
<td>20.41</td>
</tr>
</tbody>
</table>

4.2. Determination of light weight particles

As per ASTM C 123 the presence of light weight particles is done. The percentage of light weight particles is 5% which is very lean to consider.

4.3. Physical properties

The Table 3 indicates the water absorption of Steel slag is around 1% higher than that of natural aggregate which in turn will affect the workability of the concrete. The bulk density result indicates steel sag is heavier than natural coarse aggregate. The specific gravity of steel slag and natural coarse aggregate has very thin difference only.

<table>
<thead>
<tr>
<th>Test</th>
<th>Coarse Aggregate</th>
<th>Steel Slag</th>
</tr>
</thead>
<tbody>
<tr>
<td>Specific gravity</td>
<td>2.75</td>
<td>2.86</td>
</tr>
<tr>
<td>Bulk density</td>
<td>2886 kg/m³</td>
<td>3020 kg/m³</td>
</tr>
<tr>
<td>Water absorption</td>
<td>0.8%</td>
<td>1.01%</td>
</tr>
</tbody>
</table>

4.4. Mechanical properties

The mechanical properties of the aggregates influence the strength of the concrete. For making strong concrete strong aggregates are essential. From the Table 4, it is seen that steel slag produces higher results than natural aggregate for the strength tests like Crushing value, 10 percent Fines Value and Impact Value.

<table>
<thead>
<tr>
<th>Test</th>
<th>Coarse Aggregate</th>
<th>Steel Slag</th>
<th>Limiting Value as per IS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Crushing Value</td>
<td>6.55%</td>
<td>8%</td>
<td>Not more than 30%</td>
</tr>
<tr>
<td>10 percent Fines value</td>
<td>7.8%</td>
<td>8.3%</td>
<td>7.5% to 12.5%</td>
</tr>
<tr>
<td>Impact value</td>
<td>22.87%</td>
<td>29.57%</td>
<td>Less than 30%</td>
</tr>
<tr>
<td>Los Angeles’s Abrasion</td>
<td>8.27%</td>
<td>1.16%</td>
<td>Not more than 50%</td>
</tr>
<tr>
<td>Deval’s Attrition</td>
<td>18.56%</td>
<td>3.68%</td>
<td>—</td>
</tr>
</tbody>
</table>

The resistance to wear observed by Los Angeles abrasion and Deval’s Attrition shows the good performance of the steel slag than natural coarse aggregate.

4.5. Chemical test

The chemical analysis of steel slag indicates the presence of high percentage of CaO and FeO. Apart from these the steel slag also contains considerable amount of MgO. The chemical analysis of steel slag is provided in the Table 5.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Steel slag (%)</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>CaO</td>
<td>35.28</td>
<td></td>
</tr>
<tr>
<td>MgO</td>
<td>9.27</td>
<td></td>
</tr>
<tr>
<td>SiO₂</td>
<td>16.69</td>
<td></td>
</tr>
<tr>
<td>Al₂O₃</td>
<td>6.20</td>
<td></td>
</tr>
<tr>
<td>MnO</td>
<td>1.88</td>
<td></td>
</tr>
<tr>
<td>FeO</td>
<td>26.91</td>
<td></td>
</tr>
<tr>
<td>P₂O₅</td>
<td>1.43</td>
<td></td>
</tr>
<tr>
<td>Na₂O</td>
<td>0.16</td>
<td></td>
</tr>
<tr>
<td>K₂O</td>
<td>0.03</td>
<td></td>
</tr>
<tr>
<td>SO₃</td>
<td>0.56</td>
<td></td>
</tr>
</tbody>
</table>

5. Mix Design

The mix design for concrete M30 grade is arrived based on the code IS 10262:2009, and the obtained mix proportion is 1:1.45:2.62 and water cement ratio is 0.45.

6. Proposed Fuzzy System

The proposed fuzzy system for mix design of concrete was shown in Fig. 1. The integrated system is composed of the following sub-fuzzy systems:

- **CS system**: compressive strength sub-fuzzy system is designed to quantify the target compressive strength.
- **W/C system**: Water/cement ratio sub-fuzzy system is designed to determine the water-to-cement ratio of required grade of concrete.
- **IGC system**: Ideal grading curve sub-fuzzy system is designed to estimates the volume of coarse and fine aggregate and draw an ideal grading curve.
- **FW system**: Free water sub-fuzzy system designed to estimate the available free water of concrete.

Each sub-fuzzy system decomposes the input and output variables by using fuzzy membership functions. Trapezoidal and triangular membership functions are used and the sub-fuzzy system generated, are Mamdani type. The design and implementation of inference system are done in MATLAB software with its fuzzy logic toolbox.
6.1. Compressive Strength Sub-Fuzzy System (CS System)

CS system (Compressive Strength Sub-Fuzzy System) quantifies the target compressive strength of concrete at the age of 28 days ($f_{cm}$). This system uses two fuzzy variables as the target compressive strength of concrete. $Q$ is the quality of the concrete and $f_c$ is the compressive strength and yield on target compressive strength as output ($f_{cm}$). The set defined for $Q$ is:

$$Q = \{HQ, MQ, LQ\}$$

Where $HQ, MQ$ and $LQ$ are high quality, moderate quality and low quality of concrete, respectively.

The fuzzy label $f_c$ is the set:

$$f_c = \{M15, M20, M25, M30, M35, M40\}$$

For example, M20 label represents an approximate specific compressive strength of 20 MPa at the age of 28 days. The output fuzzy label ($f_{cm}$) is defined in the following set:

$$f_{cm} = \{T20, T24, T27, T31, T36, T40, T43, T48, T51\}$$

The fuzzy inference system has 18 rules, all of which were achieved experience in concrete mix design. Membership functions for the input and output parameters for the CS system are shown in Fig. 2. The output of the CS system as $f_{cm}$ surface of the combined effects of $f_c$ and $Q$ are shown in Fig. 3.
6.2. Water/Cement Ratio Sub-Fuzzy System
(W/C System)

This system uses three linguistic inputs with output water-to-cement ratio of required grade of concrete. The first input is \( f_{cm} \) which is obtained from CS system the second input is cement type with fuzzy label:

\[
\text{Cement type} = \{C43, C53\}
\]

Where C43 and C53 have cement mortar strength of 43 and 53 kg/cm\(^2\) at 28 days. The third input is environmental conditions and their fuzzy labels set are:

\[
\text{Environmental condition} = \{M_{i}, M_{o}, S_{e}, V_{s}e, E_{x}\}
\]

Where \( M_{i}, M_{o}, S_{e}, V_{s}e \) and \( E_{x} \) are mild, moderate, severe, very severe and extreme environmental conditions respectively. The fuzzy inference system is given 75 rules. The output fuzzy label set of the systems are:

\[
\text{W/C} = \{0.40, 0.41, \ldots, 0.54, 0.55\}
\]

For example 0.40 of W/C represents that the water to cement ratio is 0.40. Membership functions for the input and output parameters for the W/C system are shown in Fig. 4. The output of the W/C system as W/C surface of the combined inputs is shown in Fig. 5 as a 3D surfaces.
Fig. 4. Input and output variables of $W/C$ system to determine the water to cement ratio

Fig. 5. Output of $W/C$ system for combined effect of: a) environmental condition and cement type on $W/C$; b) $f_{cm}$ and cement type on $W/C$; c) MSA and cement type on $W/C$
6.3. Ideal Grading Curve Sub-Fuzzy System (IGC System)

The aggregate grading curve should be modified and an optimized ratio of fine aggregate to coarse aggregate is chosen for maximum packing density. The ideal grading curve can be arrived by using the modified Fuller-Thompson relationship by defining power parameter $n$ as:

$$P = \frac{100\%}{(1 - (0.075/D)^n)} \times \left( \frac{d}{D} \right)^n - (0.075/D)^n$$  \hspace{1cm} (7)

Where $P$ is the cumulative passing percentage from a sieve, $d$ is the sieve size and $D$ is the maximum size of aggregate (MSA). Parameter $n$ specifies the properties of ideal aggregate grading to maximize packing density. The input and output variables are to be trained in sub fuzzy system and they are defined as

$$MSA = \{MSA_{4.75}, MSA_{10}, MSA_{12.5}, MSA_{20}\}$$  \hspace{1cm} (8)

$$Slump\ level = \{Very\ Low, Low, Medium, High\}$$  \hspace{1cm} (9)

Slump level is followed by using IS 456:2000 provisions. Where very low, low, medium and high are slump values of >25 mm, 25 mm-75 mm, 50 mm-100 mm and 100 mm-150 mm respectively.

$$n = \{n0.1, n0.15, n0.2, n0.25, n0.3, n0.35, n0.4, n0.45, n0.5, n0.55, n0.6, n0.67\}$$  \hspace{1cm} (10)

For example, $n0.25$ means that the power of $n$ equals 0.25. There are 48 defined rules. Fig. 6 shows the combined effects of slump and maximum size of aggregate on selection of $n$. After developing the value of $n$ as the output of IGC sub-fuzzy system, it is used in the Fuller-Thompson relationship (Eq. 8) to develop an ideal grading curve. Fig. 7 is an example of such a curve for $MSA = 20\ mm$ ($MSA_{20}$) and $n = 0.427$. The output of IGC system due to combined effect of maximum size of aggregate and slump value is shown in Fig. 8.

6.4. Free Water Sub-Fuzzy System (FW System)

FW system determines the available free water of concrete. It has two linguistic input variables with output free water. The first input, fineness modulus ($FM$) is obtained from IGC system and second input is target slump value. The fuzzy label set for $FM$ is:

$$FM = \{FM_3, FM_{3.5}, FM_4, FM_{4.5}, FM_5, FM_{5.5}, FM_6, FM_{6.5}, FM_7\}$$  \hspace{1cm} (11)

For example $FM_{4.5}$ means, the fineness modulus of aggregate is 4.5. The second input, slump value is obtained from Eq. 9. 36 rules are given as input for the fuzzy inference. The outputs of the fuzzy system are:

$$Free\ water = \{150, 160, 170, 180, \ldots, 230, 240, 250\}$$  \hspace{1cm} (12)

For example 150 in the Eq. 12 represents the free water content per unit volume is 150. Membership functions for the input and output parameters for the FW system are shown in Fig. 9. The output of the FW system due to the combined effects of slump level and fineness modulus is shown in Fig. 10.

The cement content per unit volume of concrete can be calculated by using water to cement ratio obtained from $W/C\ SYSTEM$ and free water content per unit volume from FW SYSTEM.

$$Cement\ content\ per\ unit\ volume = \frac{Free\ water\ per\ unit\ volume}{(Water\ to\ cement\ ratio)}$$  \hspace{1cm} (13)

With the quantities of free water content and cement content obtained from Eq. 13, the total aggregate content per unit volume of concrete can be calculated from the following equation.

$$V = \left[ W + \frac{(C/S_c) + (A/S_a)}{1000} \right]$$  \hspace{1cm} (14)

Where, $V$ is volume of fresh concrete ($m^3$) minus volume of entrapped air, $W$ is water content per unit volume ($m^3$) of concrete, $C$ is cement content per unit volume ($m^3$) of concrete, $S_c$ is specific gravity of cement, $A$ is total aggregate per unit volume ($m^3$) and $S_a$ is specific gravity of aggregate.
7. Results and discussion

7.1. Material properties

From the mechanical tests of coarse aggregate for concrete, it is clearly seen that the steel slag aggregates outperform the natural aggregates. The steel slag aggregate can be referred as a coarse aggregate suitable for concrete.

7.2. Ideal Grading Curve

The cumulative percentage passing in each sieve as per proposed ideal grading curve and for aggregates used in M30 concrete as per IS method are calculated by using the curves shown in Fig. 7 and are shown in Table 6. The continuous particle size distribution enables higher packing density and improves the concrete properties.

7.3. Validation and Feasibility of Fuzzy System

The feasibility of the proposed fuzzy system is evaluated by comparing the mix proportions and performance with that of conventional IS method for 0%, 10%, 20%, 30%, 40%, 50%, 60%, 70%, 80%, 90% and 100% replacement by steel slag. The water cement ratio of fuzzy model is less which is reflected in the free water content. From Table 7, it can be observed...
TABLE 6
Comparison of Weight Retained

<table>
<thead>
<tr>
<th>Sieve size (mm)</th>
<th>Cumulative Percentage passing</th>
<th>For aggregates used in M30 concrete as per IS method</th>
</tr>
</thead>
<tbody>
<tr>
<td>20</td>
<td>100</td>
<td>96.5</td>
</tr>
<tr>
<td>10</td>
<td>66.9</td>
<td>40</td>
</tr>
<tr>
<td>4.75</td>
<td>46.9</td>
<td>33</td>
</tr>
<tr>
<td>2.36</td>
<td>28.7</td>
<td>31.4</td>
</tr>
<tr>
<td>1.18</td>
<td>18.6</td>
<td>23</td>
</tr>
<tr>
<td>0.6</td>
<td>11.4</td>
<td>10.3</td>
</tr>
<tr>
<td>0.3</td>
<td>6.1</td>
<td>1.7</td>
</tr>
<tr>
<td>0.15</td>
<td>2.2</td>
<td>0</td>
</tr>
<tr>
<td>0.075</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>R²</td>
<td>0.985</td>
<td>0.916</td>
</tr>
</tbody>
</table>

Fig. 9. Input and output parameters of FW system to determine free water content

Fig. 10. Combined effects of slump and Fineness Modulus

that for the same volume of concrete, the weight of cement, coarse aggregate and fine aggregate as per fuzzy model are higher than that of IS method. Therefore it can be concluded that the bulk density of Fuzzy model is greater than that of IS method.

TABLE 7
Mix Design of Fuzzy Model versus IS Method

<table>
<thead>
<tr>
<th>Percentage replacement</th>
<th>As per W/C ratio</th>
<th>Cement (kg/m³)</th>
<th>Coarse aggregate (kg/m³)</th>
<th>Fine aggregate (kg/m³)</th>
<th>Free water (kg/m³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0% to 100% (10% increments)</td>
<td>Fuzzy model</td>
<td>0.44</td>
<td>443</td>
<td>1152.1</td>
<td>639.7</td>
</tr>
<tr>
<td>IS</td>
<td>0.45</td>
<td>438</td>
<td>1148.6</td>
<td>637.8</td>
<td>197</td>
</tr>
</tbody>
</table>
The Fig. 11 and Fig. 12 show the compressive strength and bulk density of concrete cube as per proposed fuzzy model and IS method. Hardened concrete is tested for bulk density as per IS 1199 and Compressive Strength as per IS516:1959. The bulk density of fuzzy model shows considerable increase due to improved packing density of aggregates by following the Fuller Thomson curve. The compressive strength of Fuzzy model is higher than those of IS method due to high packing density. It is observed that, all percentage replacement levels show considerable increase in compressive strength and bulk density in Fuzzy model.

8. Conclusions

- The concrete mix proportion of the given fuzzy model agrees with IS method and its comparatively better.

- As a result of developing ideal grading curve in fuzzy model, the proposed fuzzy model has increased compressive strength than IS method.

- A comparison of results from the proposed fuzzy model with those from the IS method indicates increased bulk density which is understandable from 3% increase in bulk density of fuzzy model than that of IS method in 0% replacement.

- In both proposed fuzzy system and IS method, there is a remarkable increase in compressive strength and bulk density, with increment in the percentage replacement of steel slag.

- From the increased compressive strength for 100% replacement by steel slag, it can be concluded that that steel is better alternate material for natural coarse aggregate.
Acknowledgement

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REFERENCES